

55. 分数式の計算②

(1) $\frac{x-3}{x-2}$	(2) 1	(3) $\frac{x}{x-3}$	(4) $\frac{a-b+c}{a+b+c}$	(5) $\frac{x+y}{x-y}$	(6) $\frac{2x+3}{x+1}$
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次の式を計算せよ。

$$(1) \frac{x^2-2x-3}{x^2-x-2} = \frac{(x-3)\cancel{(x+1)}}{(x-2)\cancel{(x+1)}} = \frac{x-3}{x-2}$$

$$(2) \frac{x^2+3x+2}{x^2-4} \times \frac{x-2}{x+1} = \frac{\cancel{(x+1)}(x+2)}{\cancel{(x+2)}\cancel{(x-2)}} \times \frac{\cancel{x-2}}{\cancel{x+1}} = 1$$

$$(3) \frac{x^2-11x+24}{x^2-6x-16} \times \frac{x^2+2x}{x^2-6x+9} = \frac{\cancel{(x-3)}\cancel{(x-8)}}{\cancel{(x-8)}\cancel{(x+2)}} \times \frac{x\cancel{(x+2)}}{\cancel{(x-3)}^x} = \frac{x}{x-3}$$

$$(4) \frac{a^2-(b-c)^2}{(a+b)^2-c^2} = \frac{\{a+(b-c)\}\{a-(b-c)\}}{\{(a+b)+c\}\{(a+b)-c\}} = \frac{\cancel{(a+b-c)}(a-b+c)}{(a+b+c)\cancel{(a+b-c)}} = \frac{a-b+c}{a+b+c}$$

$$(5) \frac{x^2+xy+y^2}{x^2-xy+y^2} \div \frac{x^3-y^3}{x^3+y^3} = \frac{x^2+xy+y^2}{x^2-xy+y^2} \div \frac{(x-y)(x^2+xy+y^2)}{(x+y)(x^2-xy+y^2)}$$

$$= \frac{\cancel{x^2+xy+y^2}}{\cancel{x^2-xy+y^2}} \times \frac{(x+y)\cancel{(x^2-xy+y^2)}}{(x-y)\cancel{(x^2+xy+y^2)}}$$

$$= \frac{x+y}{x-y}$$

$$(6) \frac{2x^2-7x+3}{x^2+x-2} \div \frac{x^2-2x-3}{x^2-4} \times \frac{2x^2+x-3}{2x^2-5x+2} = \frac{\cancel{(2x-1)}(x-3)}{(x+2)\cancel{(x-1)}} \div \frac{(x-3)(x+1)}{(x+2)(x-2)} \times \frac{\cancel{(2x+3)}\cancel{(x-1)}}{\cancel{(2x-1)}(x-2)}$$

$$= \frac{\cancel{x-3}}{\cancel{x+2}} \times \frac{\cancel{(x+2)}\cancel{(x-2)}}{\cancel{(x-3)}(x+1)} \times \frac{2x+3}{\cancel{x-2}}$$

$$= \frac{2x+3}{x+1}$$