

5.1. 多項式の因数分解⑥

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|--|------------------------------------|-----------------------------|
| (1) $(a-5)(a^2+5a+25)$ | (2) $(2x+3)(4x^2-6x+9)$ | (3) $8(2a+b)(4a^2-2ab+b^2)$ |
| (4) $3(x-3)(x^2+3x+9)$ | (5) $x(x-y)(x^2+xy+y^2)$ | |
| (6) $(2x+1)(4x^2-2x+1)(2x-1)(4x^2+2x+1)$ | (7) $(x-y+2)(x^2-2xy+y^2-2x+2y+4)$ | |
| (8) $9(x-y)(x^2-xy+y^2)$ | | |

次の式を因数分解せよ。

$$(1) a^3 - 125 = (a-5)(a^2 + 5a + 25)$$

$$(2) 8x^3 + 27 = (2x+3)(4x^2 - 6x + 9)$$

$$(3) 64a^3 + 8b^3 = 8(8a^3 + b^3)$$

$$= 8(2a+b)(4a^2 - 2ab + b^2)$$

$$(4) 3x^3 - 81 = 3(x^3 - 27)$$

$$= 3(x-3)(x^2 + 3x + 9)$$

$$(5) x^4 - xy^3 = x(x^3 - y^3)$$

$$= x(x-y)(x^2 + xy + y^2)$$

$$(6) 64x^6 - 1 = (8x^3 + 1)(8x^3 - 1)$$

$$= (2x+1)(4x^2 - 2x + 1)(2x-1)(4x^2 + 2x + 1)$$

$$(7) (x-y)^3 + 8 = \{(x-y)+2\}\{(x-y)^2 - 2(x-y) + 4\}$$

$$= (x-y+2)(x^2 - 2xy + y^2 - 2x + 2y + 4)$$

$$(8) (x-2y)^3 - (y-2x)^3 = (x-2y)^3 - (y-2x)^3$$

$$= \{(x-2y) - (y-2x)\} \times \{(x-2y)^2 + (x-2y)(y-2x) + (y-2x)^2\}$$

$$= (3x-3y) \times (3x^2 - 3xy + 3y^2)$$

$$= 9(x-y)(x^2 - xy + y^2)$$